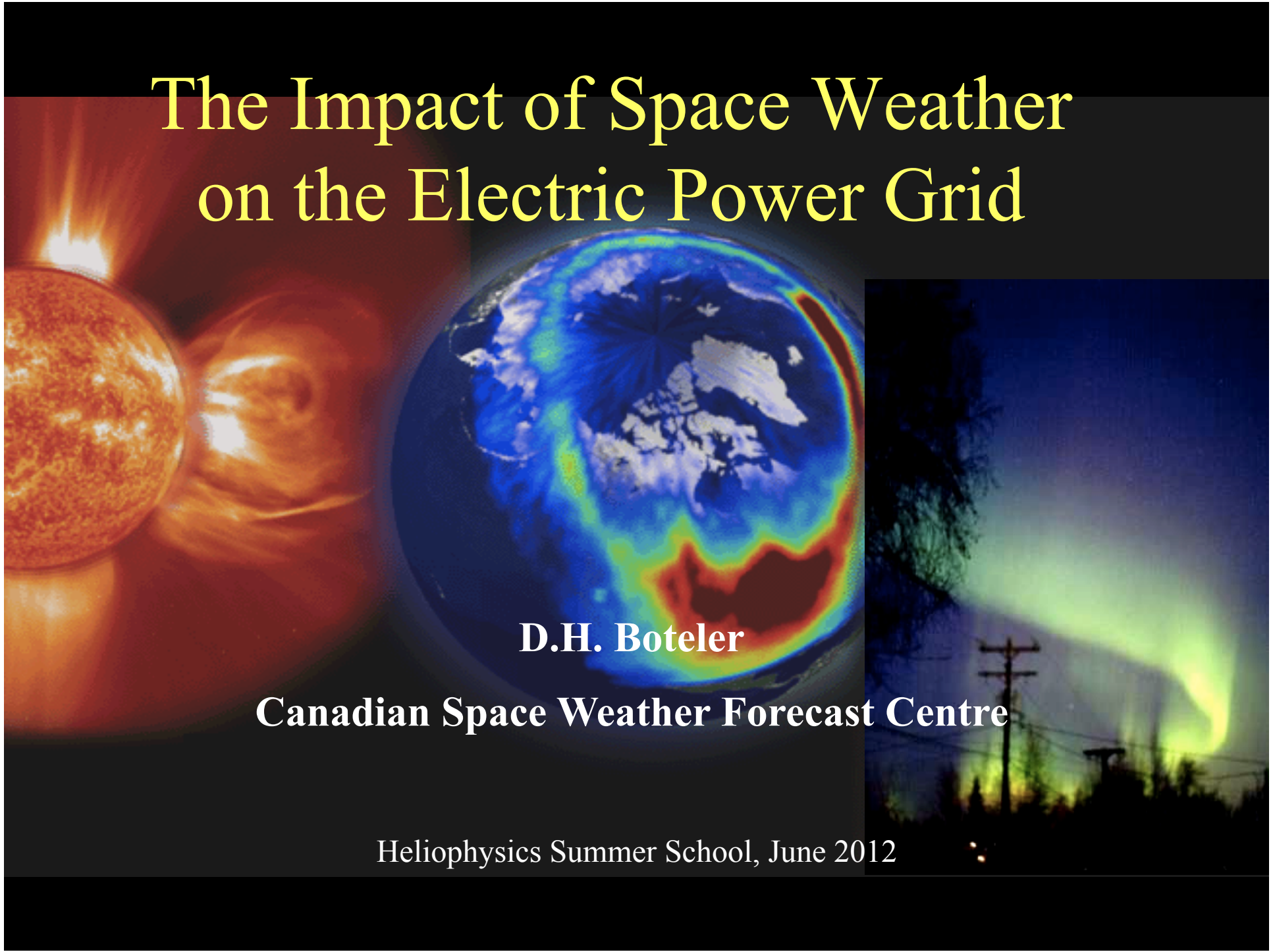


# The Impact of Space Weather on the Electric Power Grid

**D.H. Boteler**

**Canadian Space Weather Forecast Centre**

Heliophysics Summer School, June 2012

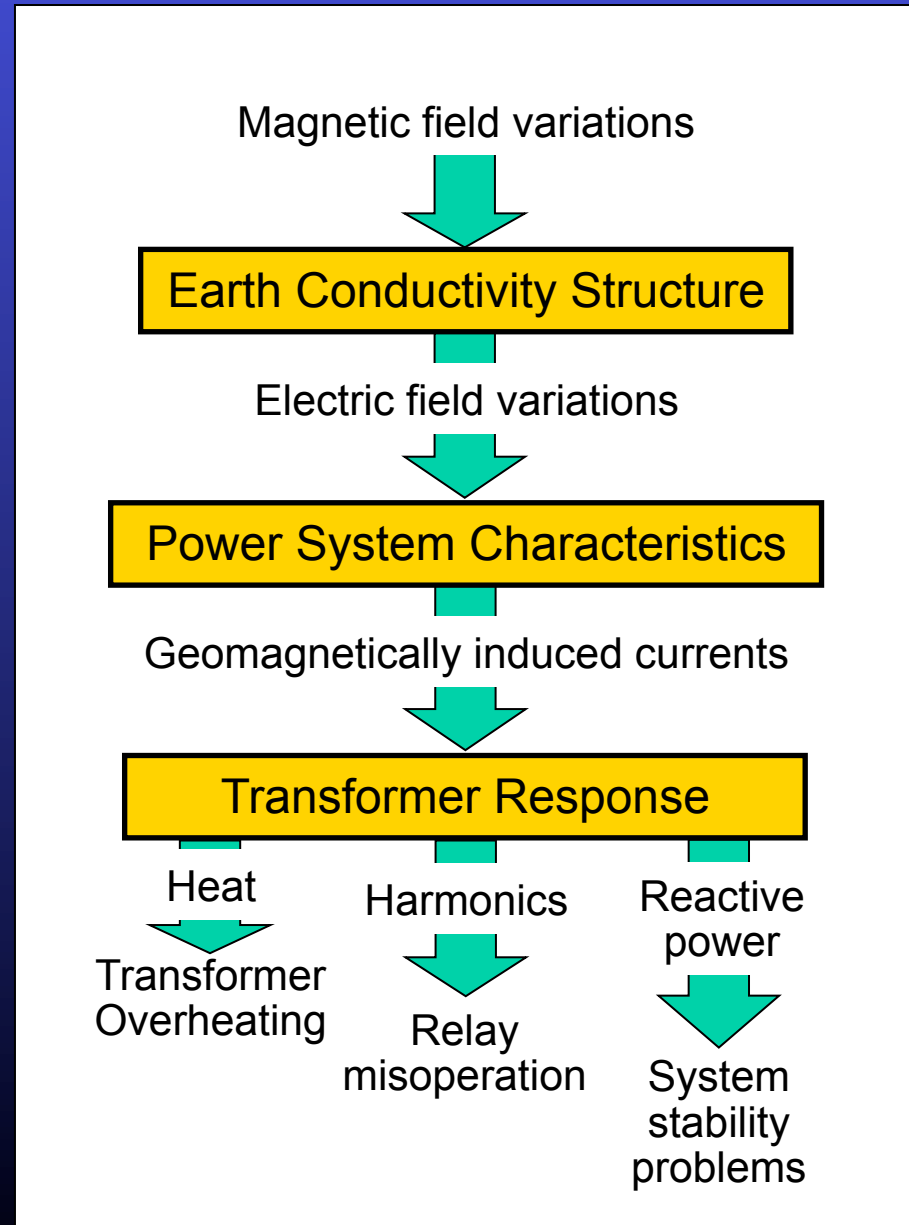


# **Hazard Assessment and Real-Time Simulation of Geomagnetically Induced Currents**

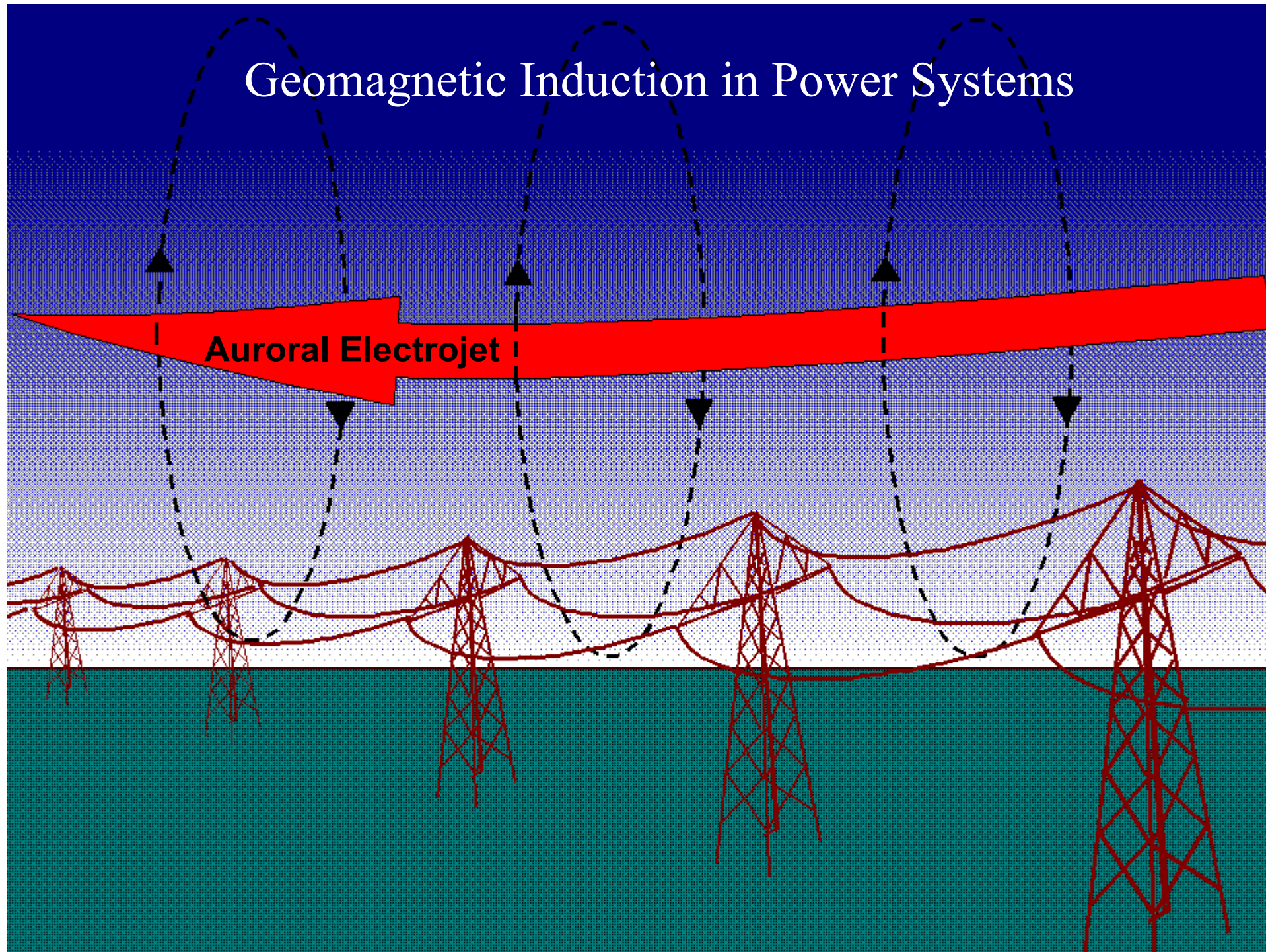
**D.H. Boteler**

**Geomagnetic Laboratory, Natural Resources Canada**

# Outline



# Geomagnetic Induction in Power Systems



# Geomagnetic Induction

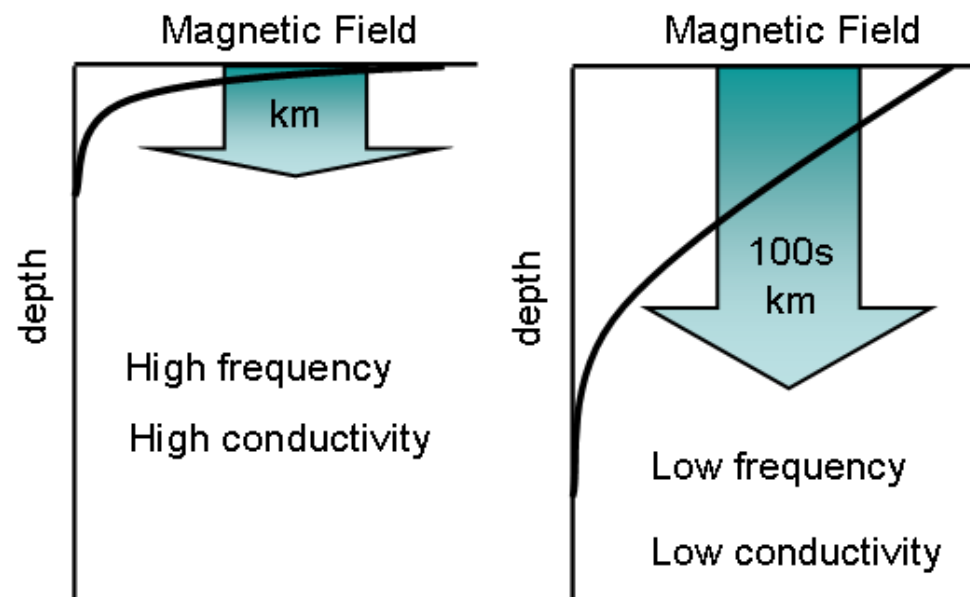
$$E \neq dB/dt$$

Induced currents create magnetic fields

Self-consistent solution where induced currents tend to cancel inducing magnetic field

Skin depth

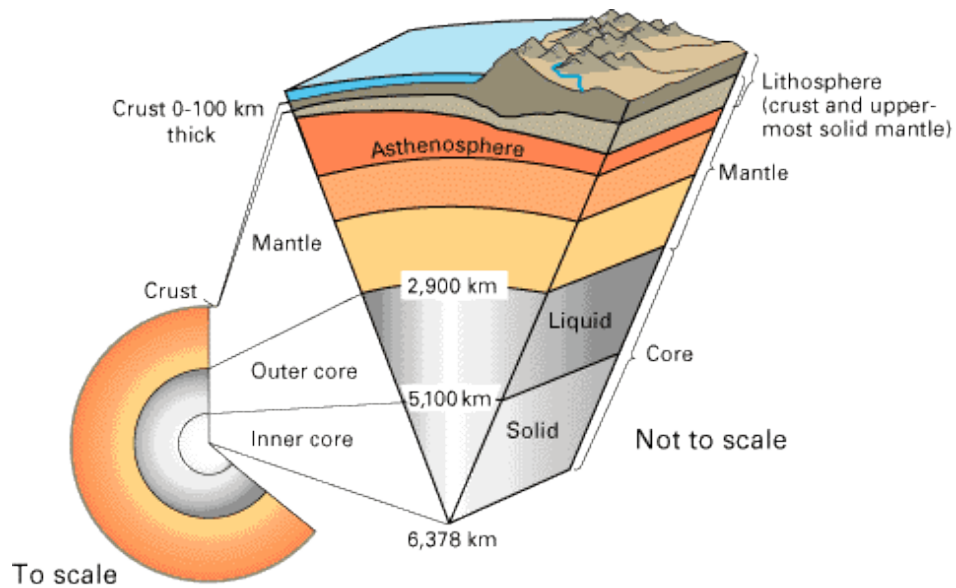
$$\delta = \sqrt{\frac{2}{\omega\mu\sigma}}$$



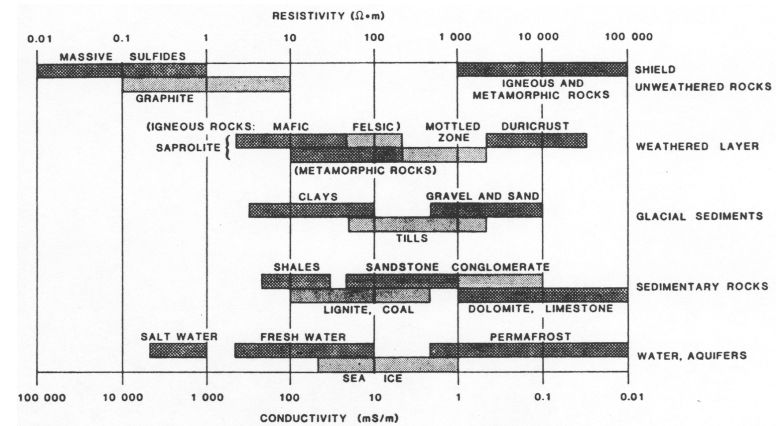


# Earth Conductivity Structure

## Earth Structure

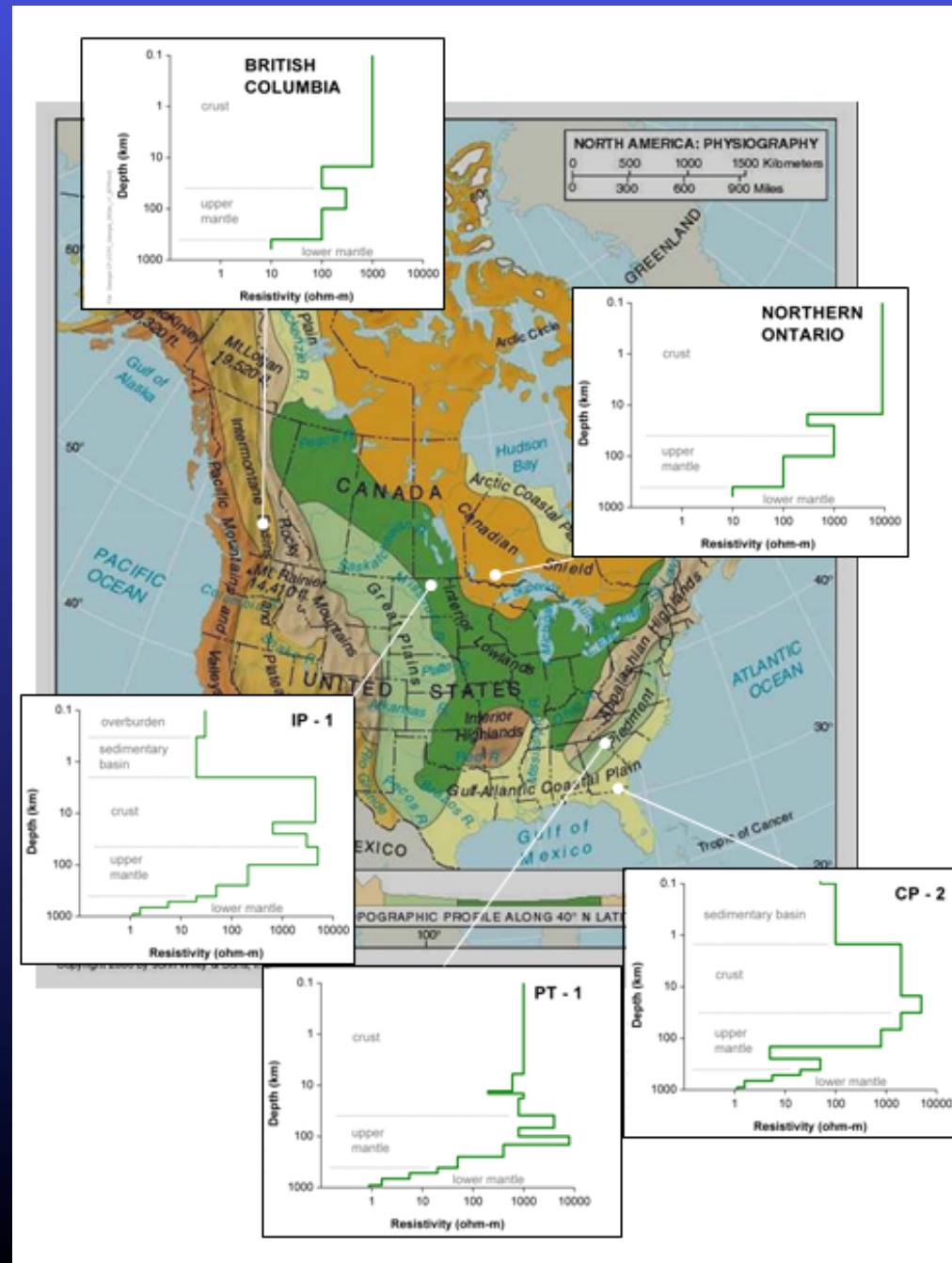


## Rock Resistivities



# Earth Models

## Examples of 1-D Conductivity Models



# Calculate Earth Response

Surface

$\sigma_1$	$d_1$
$\sigma_2$	$d_2$
$\sigma_3$	$d_3$
$\sigma_4$	$d_4$
$\sigma_5$	$d_5$
$\sigma_6$	$d_6$
$\sigma_7$	$d_\infty$

$\mu$  – permeability

$\omega$  – frequency

$Z_n$  – impedance in layer n

$\sigma_n$  – conductivity layer n

$d_n$  – depth of layer n

$k_n$  – propagation constant for layer n

Recurrence Relation

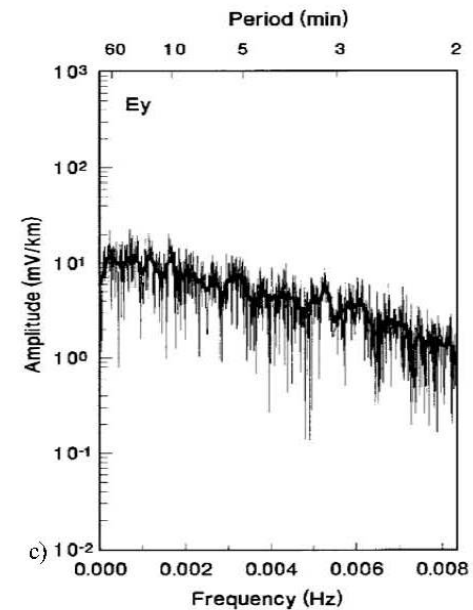
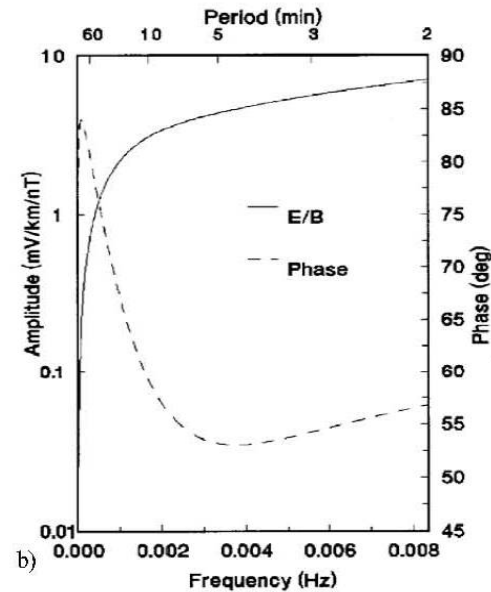
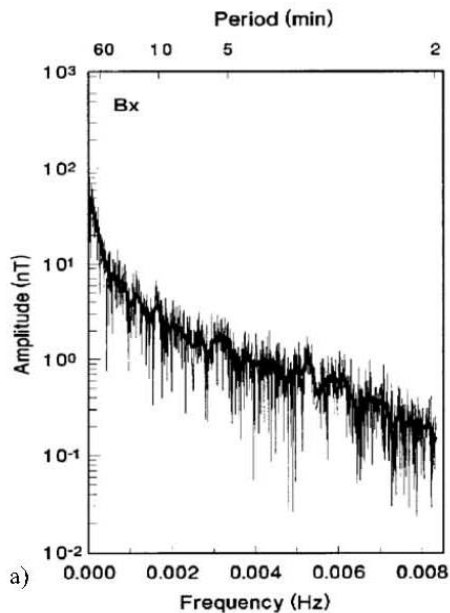
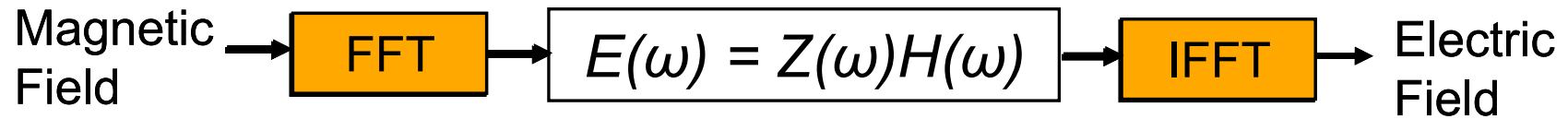
$$Z_n = i\omega\mu \left( \frac{1 - r_n e^{-2k_n d_n}}{k_n (1 + r_n e^{-2k_n d_n})} \right)$$

$$r_n = \frac{1 - k_n \frac{Z_{n-1}}{i\omega\mu}}{1 + k_n \frac{Z_{n-1}}{i\omega\mu}} \quad k_n = \sqrt{i\omega\mu\sigma_n}$$

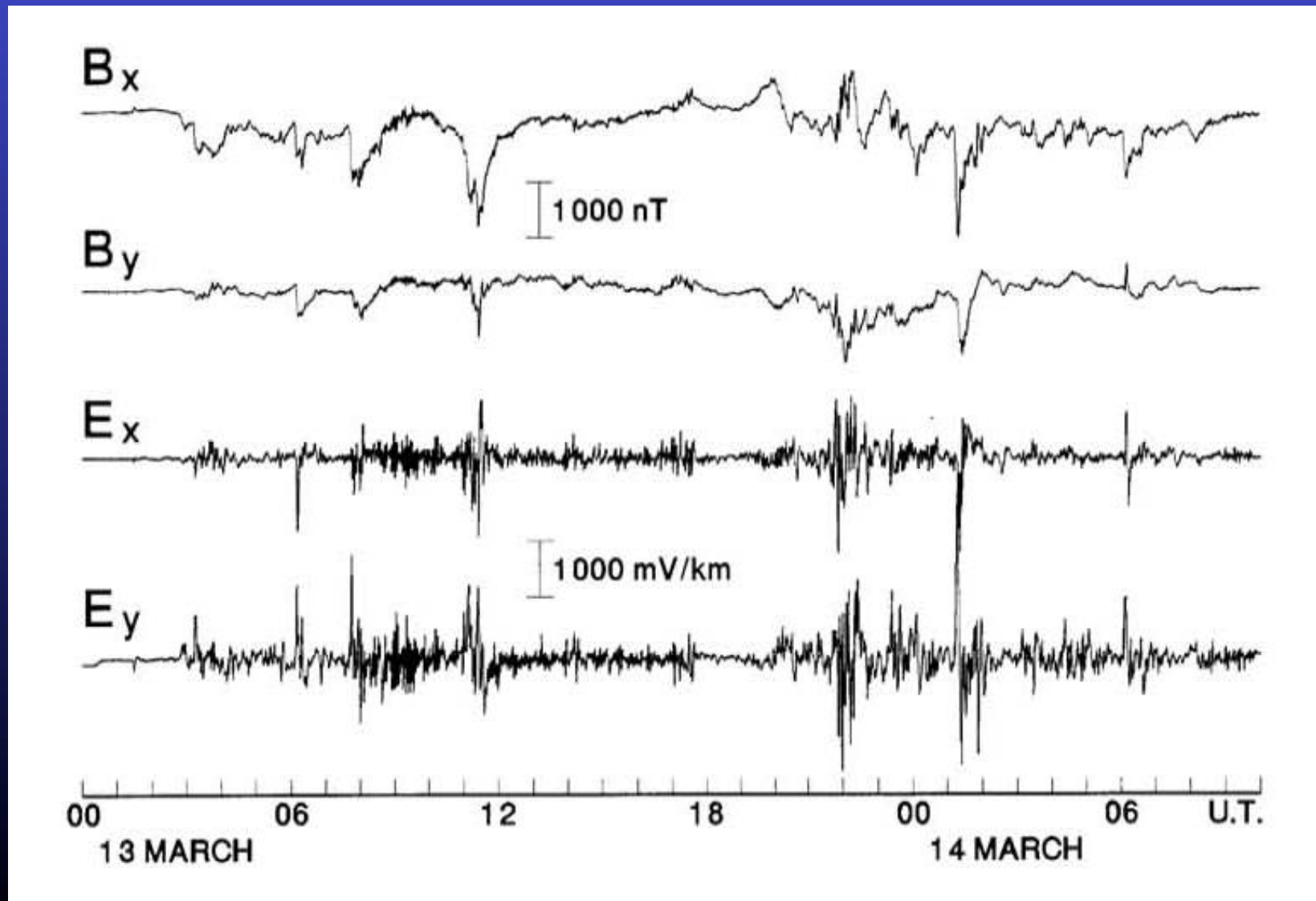
$$\text{Last layer: } Z_N = \frac{i\omega\mu}{k_N}$$



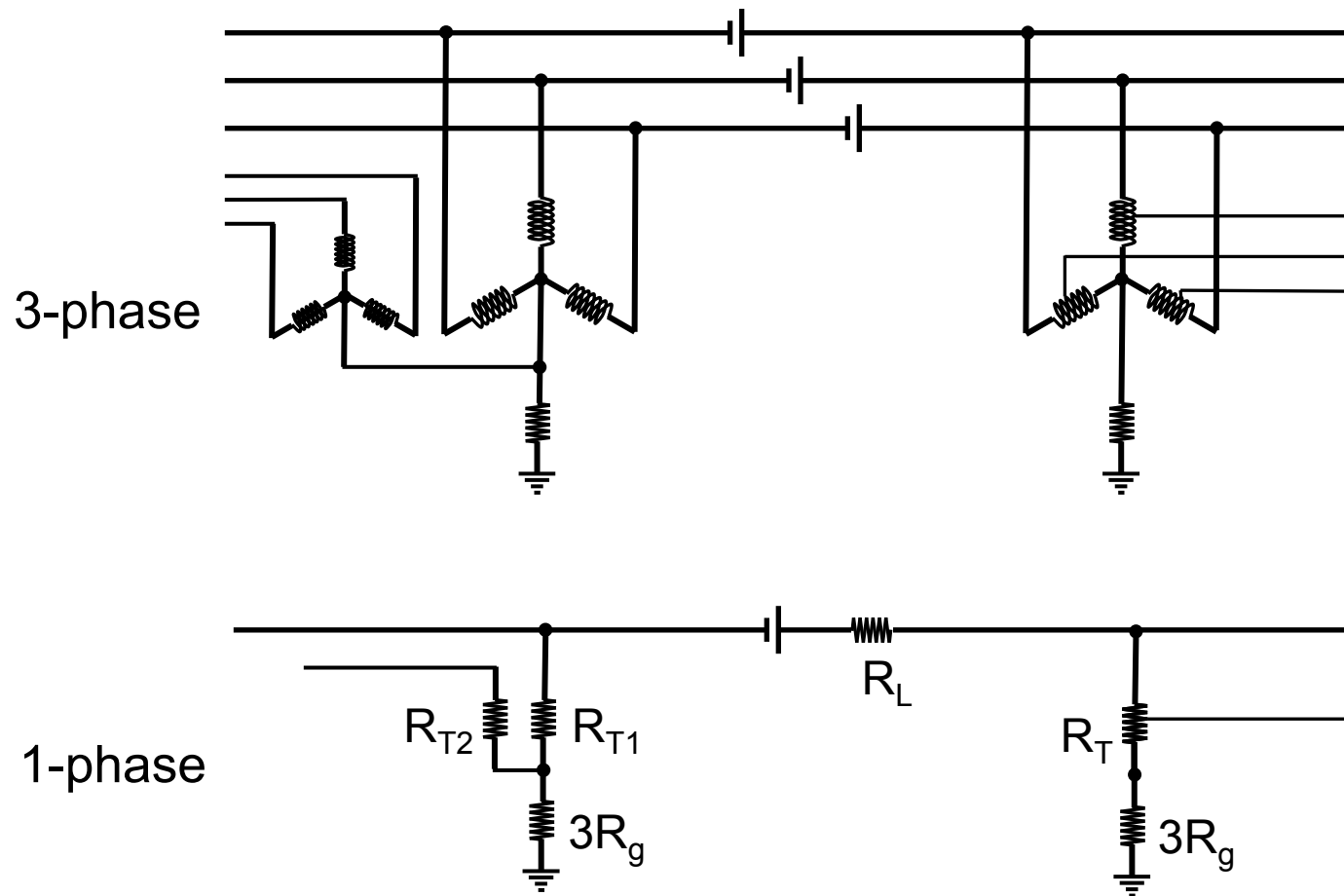
# Electric Field Calculation



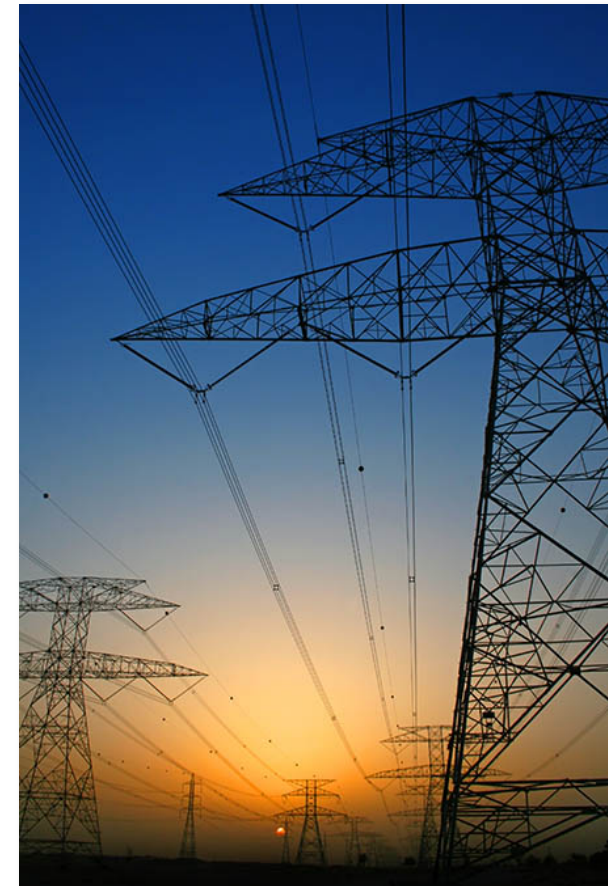
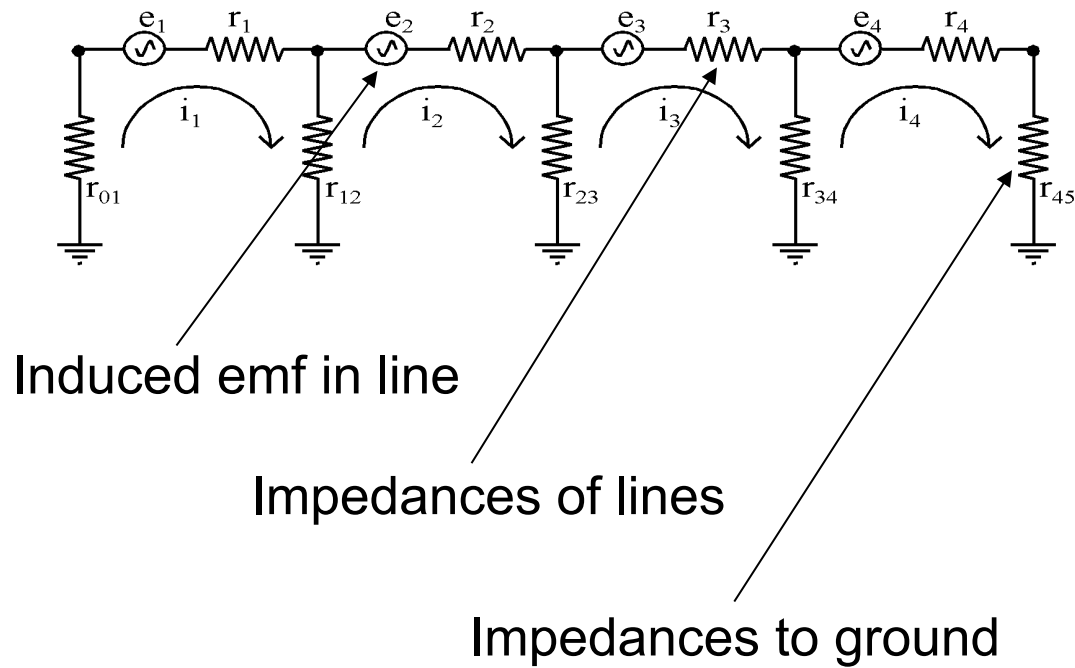
# Electric Field Calculation (Plane Wave)



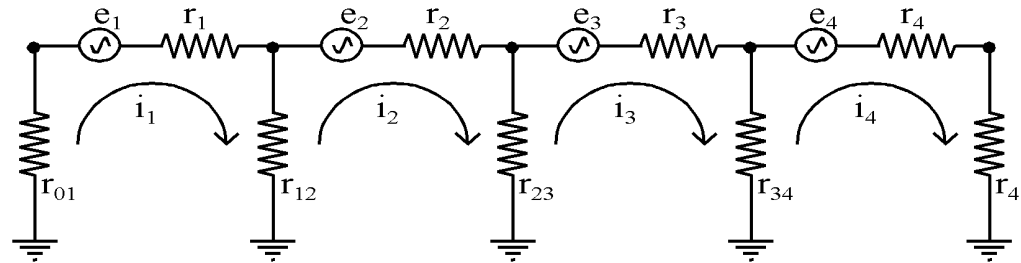
# Modelling Process: Basic Network



# Modelling Process: Basic Network



# 1. Modelling Process: Mesh Impedance Method



Using Kirchoff' s voltage law we can write equations for each loop

$$r_{01}i_1 + r_1i_1 + r_{12}(i_1 - i_2) = e_1$$

$$r_{12}(i_2 - i_1) + r_2i_2 + r_{23}(i_2 - i_3) = e_2$$

$$r_{23}(i_3 - i_2) + r_3i_3 + r_{34}(i_3 - i_4) = e_3$$

$$r_{34}(i_4 - i_3) + r_4i_4 + r_{45}i_4 = e_4$$

# 1. Modelling Process: Mesh Impedance Method

Collecting terms in  $i_1$   $i_2$  etc gives

$$(r_{01} + r_1 + r_{12})i_1 - r_{12}i_2 = e_1$$

$$-r_{12}i_1 + (r_{12} + r_2 + r_{23})i_2 - r_{23}i_3 = e_2$$

$$-r_{23}i_2 + (r_{23} + r_3 + r_{34})i_3 - r_{34}i_4 = e_3$$

$$-r_{34}i_3 + (r_{34} + r_4 + r_{45})i_4 = e_4$$

$$\begin{bmatrix} r_{01} + r_1 + r_{12} & -r_{12} & -r_{23} & 0 \\ -r_{12} & r_{12} + r_2 + r_{23} & 0 & 0 \\ 0 & -r_{23} & r_{23} + r_3 + r_{34} & -r_{34} \\ 0 & 0 & -r_{34} & r_{34} + r_4 + r_{45} \end{bmatrix} \begin{bmatrix} i_1 \\ i_2 \\ i_3 \\ i_4 \end{bmatrix} = \begin{bmatrix} e_1 \\ e_2 \\ e_3 \\ e_4 \end{bmatrix}$$



# 1. Modelling Process: Mesh Impedance Method

Thus the equations can be written in matrix form

$$[Z][I] = [E]$$

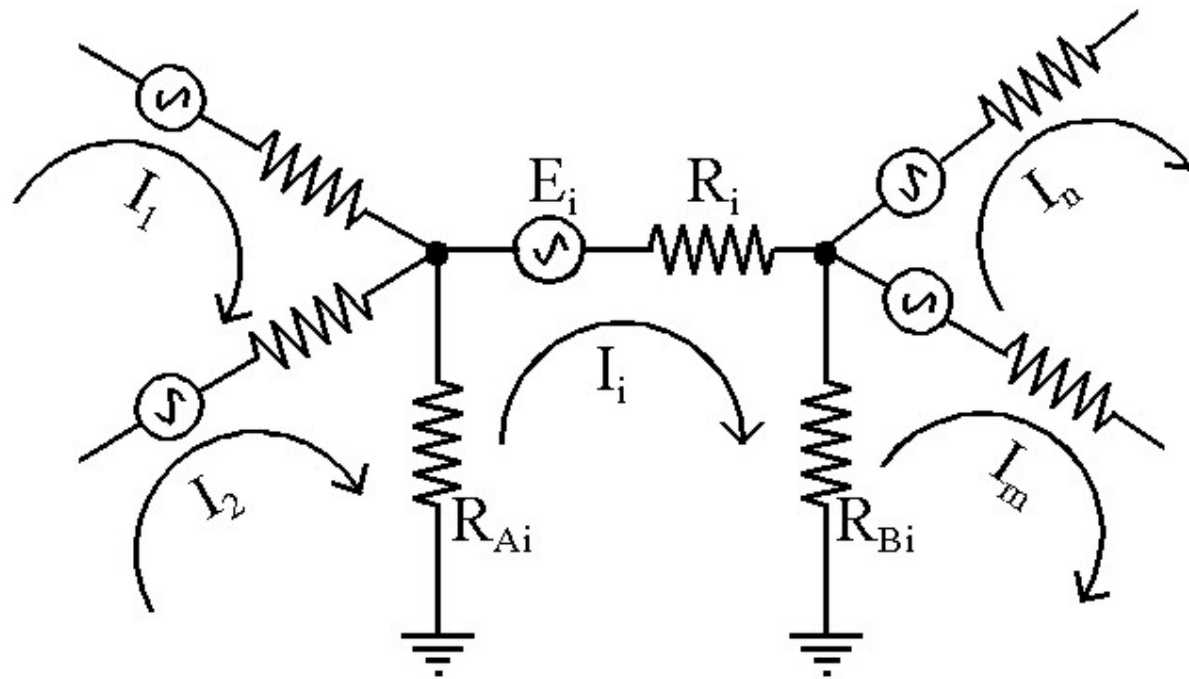
Matrix inversion then gives the expression for the currents

$$[I] = [Z]^{-1} [E]$$

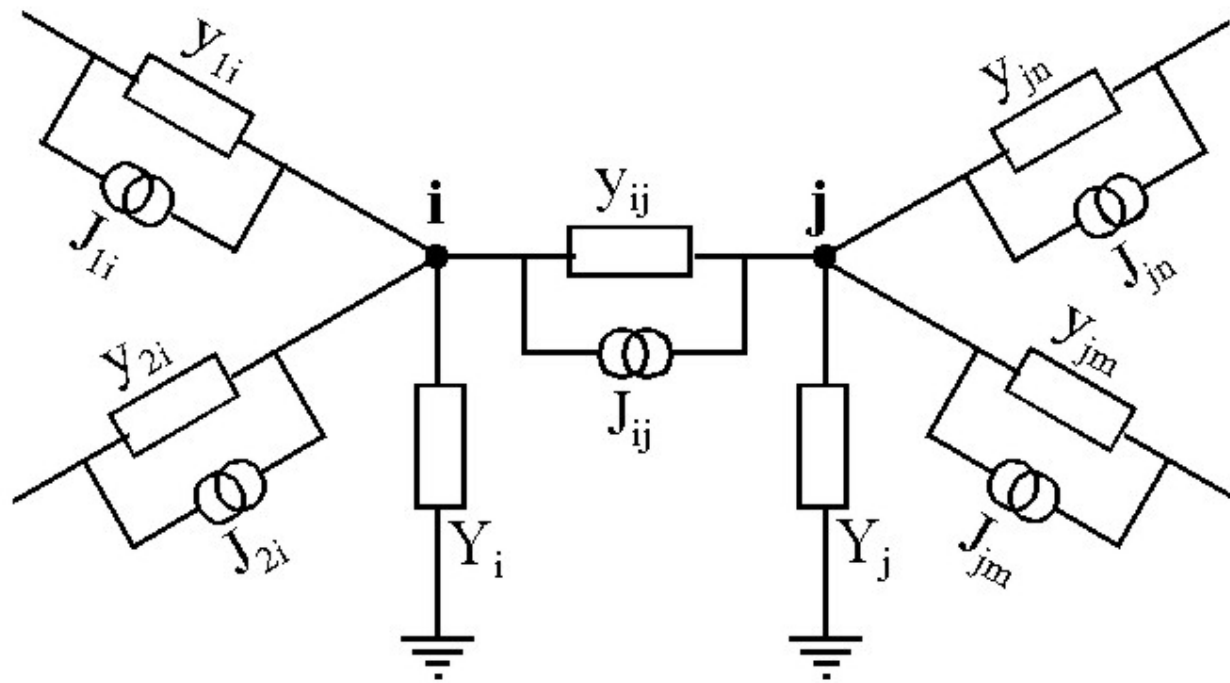
# General Modelling Methods

- Mesh Impedance Matrix Method
- Nodal Admittance Matrix Method
- Lehtinen-Pirjola Method

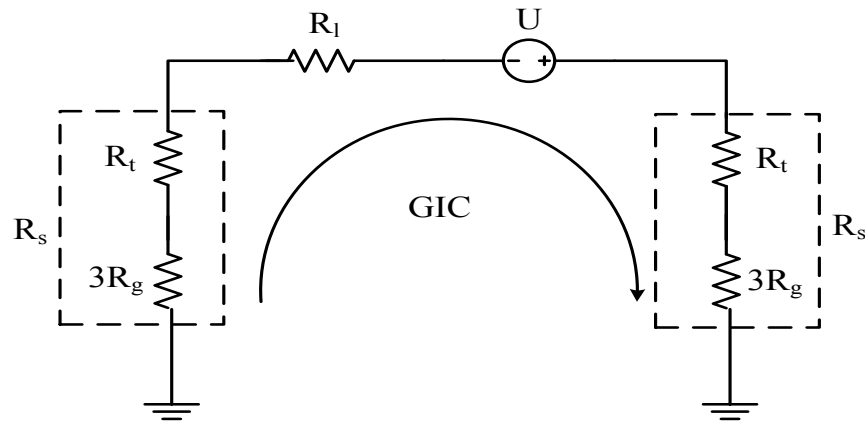
# Mesh Impedance Matrix Method



# Nodal Admittance Matrix Method



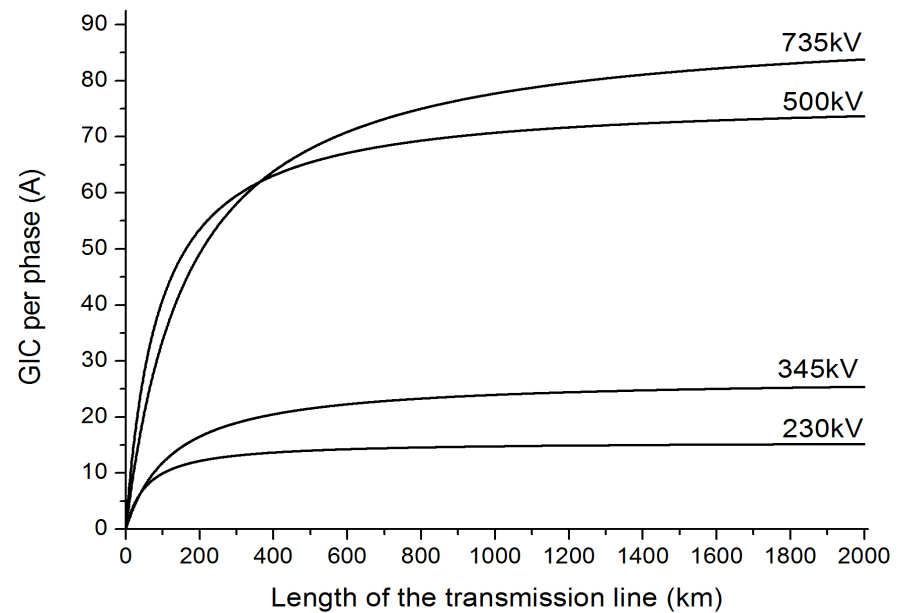
# Effect of Line Length



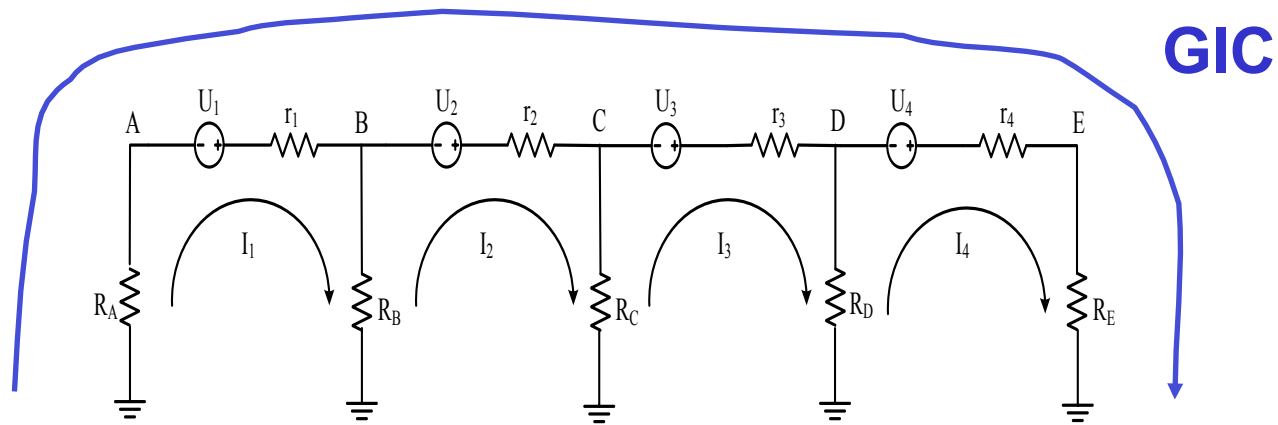
Maximum GIC

$$GIC_{\max} = \frac{E_l}{r}$$

$$GIC = \frac{U}{R_l + 2R_s} = \frac{E_l \cdot l}{r \cdot l + 2R_s}$$



# Edge Effect



GIC flows from one edge of the network to the other

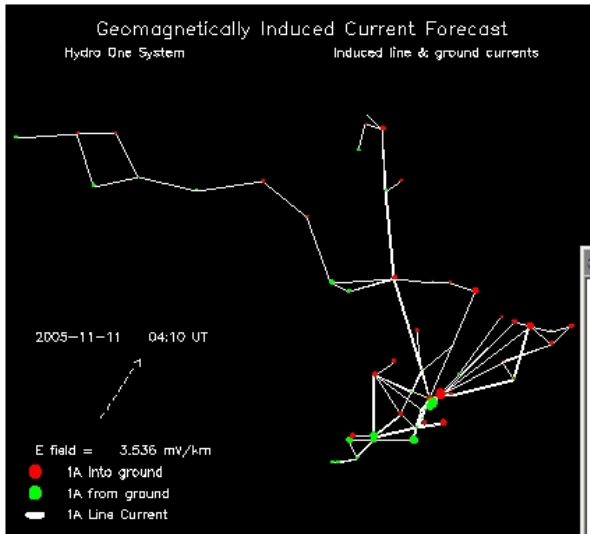
GIC flows past substations in the middle of the network



# Geomagnetically Induced Current Forecast Hydro One System

Station	Current GIC	Max GIC (Last hour)
algoma	-0.081	0.419
ansonvil	0.044	0.334
beach	0.063	1.419
beauharn	0.101	0.828
beck	0.225	2.467
bowmanv5	0.052	0.844
bruce	-0.013	2.188
bruce5	0.091	1.171
buchanan	-0.307	2.916
burlingt	-0.006	0.155
chatham	-0.055	0.437
chats_fa	0.107	0.315
chenaux	0.047	0.243
cherryw5	0.000	0.000
cherrywo	0.529	1.164
clairev5	0.000	0.000
clairevi	0.176	0.867
des_joac	0.195	0.977
detweile	0.066	0.442
dobbin	-0.044	0.256

Plot selected station GIC



GIC Region

[South&East](#)

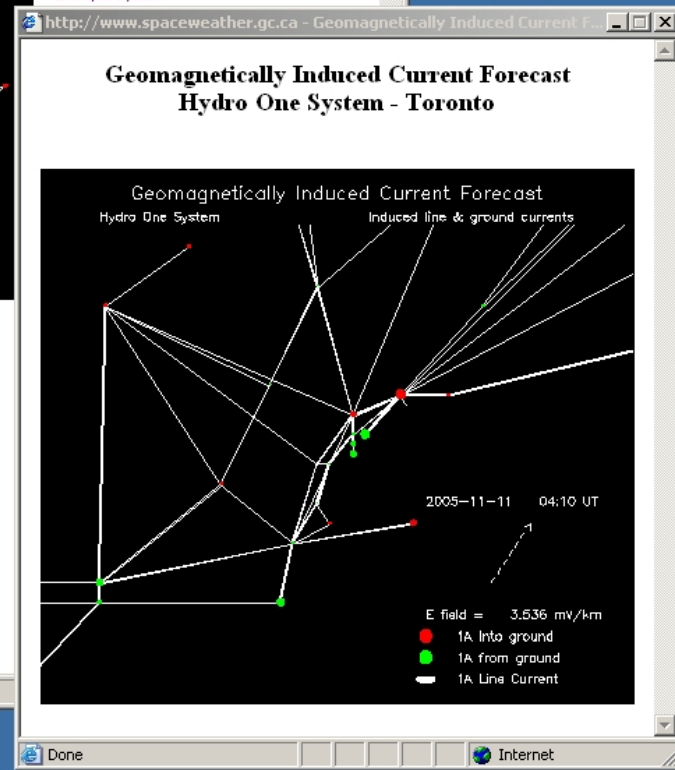
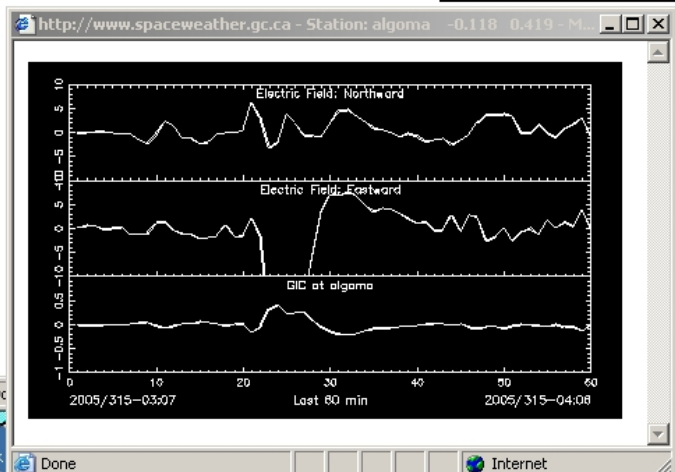
[Toronto](#)

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Information

[- Overview](#)

[- Example System](#)



GIC Simulator: Geomagnetically Induced Current Forecast - Hydro One System - Microsoft Internet Explorer

Address: [http://www.spaceweather.gc.ca/gic\\_simulator\\_e.php?gic\\_directory=GIC\\_ontariohydro](http://www.spaceweather.gc.ca/gic_simulator_e.php?gic_directory=GIC_ontariohydro)

## Geomagnetically Induced Current Forecast Hydro One System

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burlingt	-0.006	0.155
chatham	-0.055	0.437
chats_fa	0.107	0.315
chenaux	0.047	0.243
cherryw5	0.000	0.000
cherrywo	0.529	1.164
clairev5	0.000	0.000
clairevi	0.176	0.867
des_joac	0.195	0.977
detweile	0.066	0.442
dobbin	-0.044	0.256

Plot selected station GIC

Geomagnetically Induced Current Forecast  
Hydro One System  
Induced line & ground current

2005-11-11 04:10 UT

E field = 3.536 mV/km  
 ● 1A into ground  
 ● 1A from ground  
 — 1A Line Current

Station: algoma -0.118 0.419 M...

Electric Field: Northward  
 Electric Field: Eastward  
 GIC at algoma

2005/315-03:07 Last 60 min 2005/315-04:08

http://golden.spaceweather.gc.ca - Geomagnetically Induced Current Forecast - Ge...

## Geomagnetically Induced Current Forecast Generic System Theory behind Simulation - Earth Response

During a geomagnetic disturbance, the interaction of the solar wind with the Earth's magnetosphere produces electric currents that are the external source of the magnetic field variations seen at the Earth's surface. The changing magnetic field

Surface	
$\sigma_1$	$d_1$
$\sigma_2$	$d_2$
$\sigma_3$	$d_3$
$d_4$	
$d_5$	
$d_6$	
$d$	
$\infty$	

water "skin depth"  
 he skin depths range  
 response of the  
 different  
 with depth within the  
 ourier transformed to

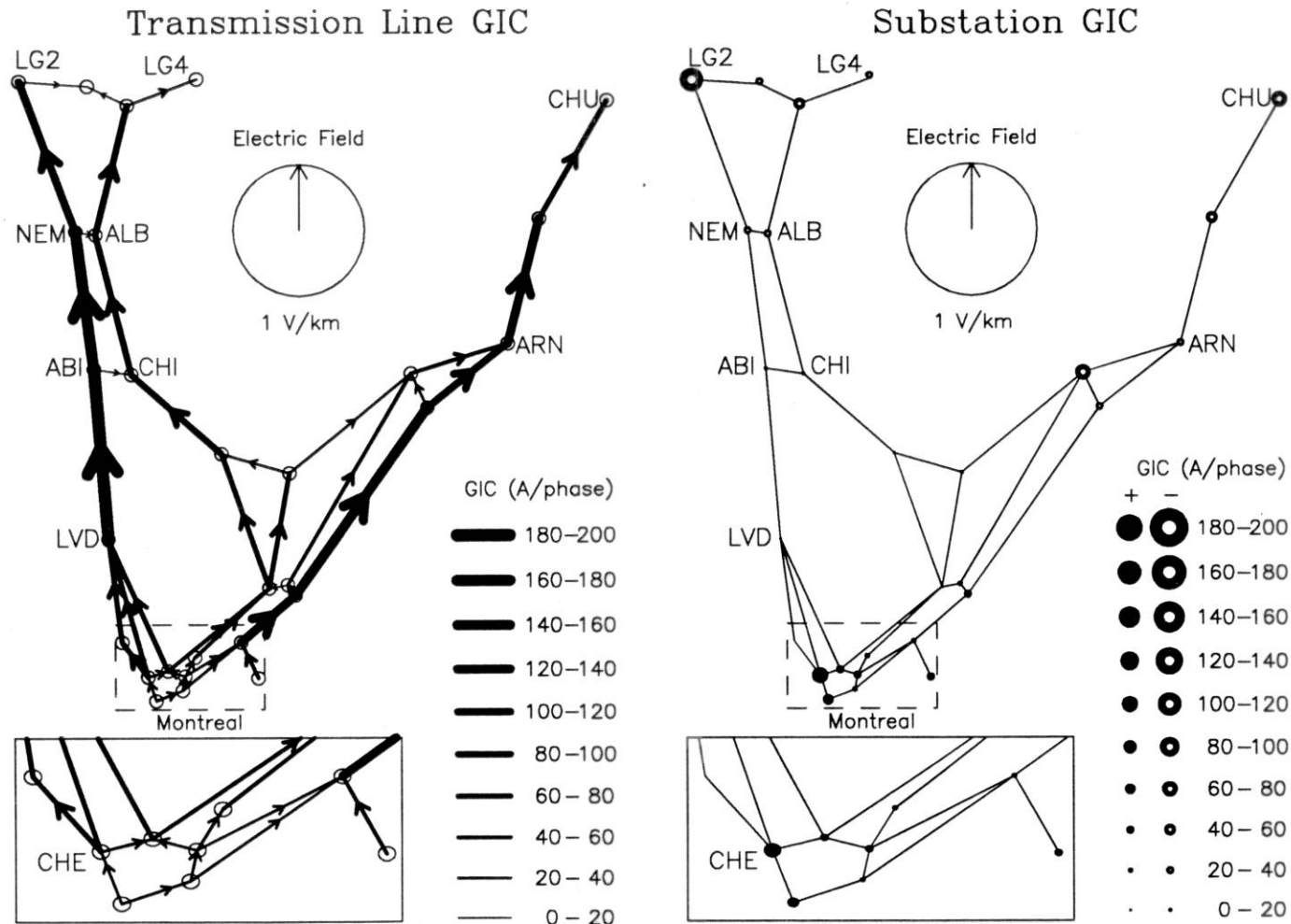
## Geomagnetically Induced Current Forecast Generic System Theory behind Simulation - Power System Model

Modelling GIC in a power system is very similar to a load-flow calculation except that the driving voltages (representing the induced geo-electric fields) are in the transmission lines between nodes, not between a node and ground. The voltage in each line is determined by integrating the electric field along the length of the line. This is converted to an equivalent current source in parallel with the line which can be represented by currents in and out of the nodes at the ends of the line. The total current into each node is obtained by summing the contributions from each line connected to that node. This becomes the input to a matrix equation featuring the resistances of the lines and the ground connections at each node. Matrix inversion is used to determine the node voltages from which it is straightforward to determine the GIC flowing in each line between nodes and in each connection between node and ground.

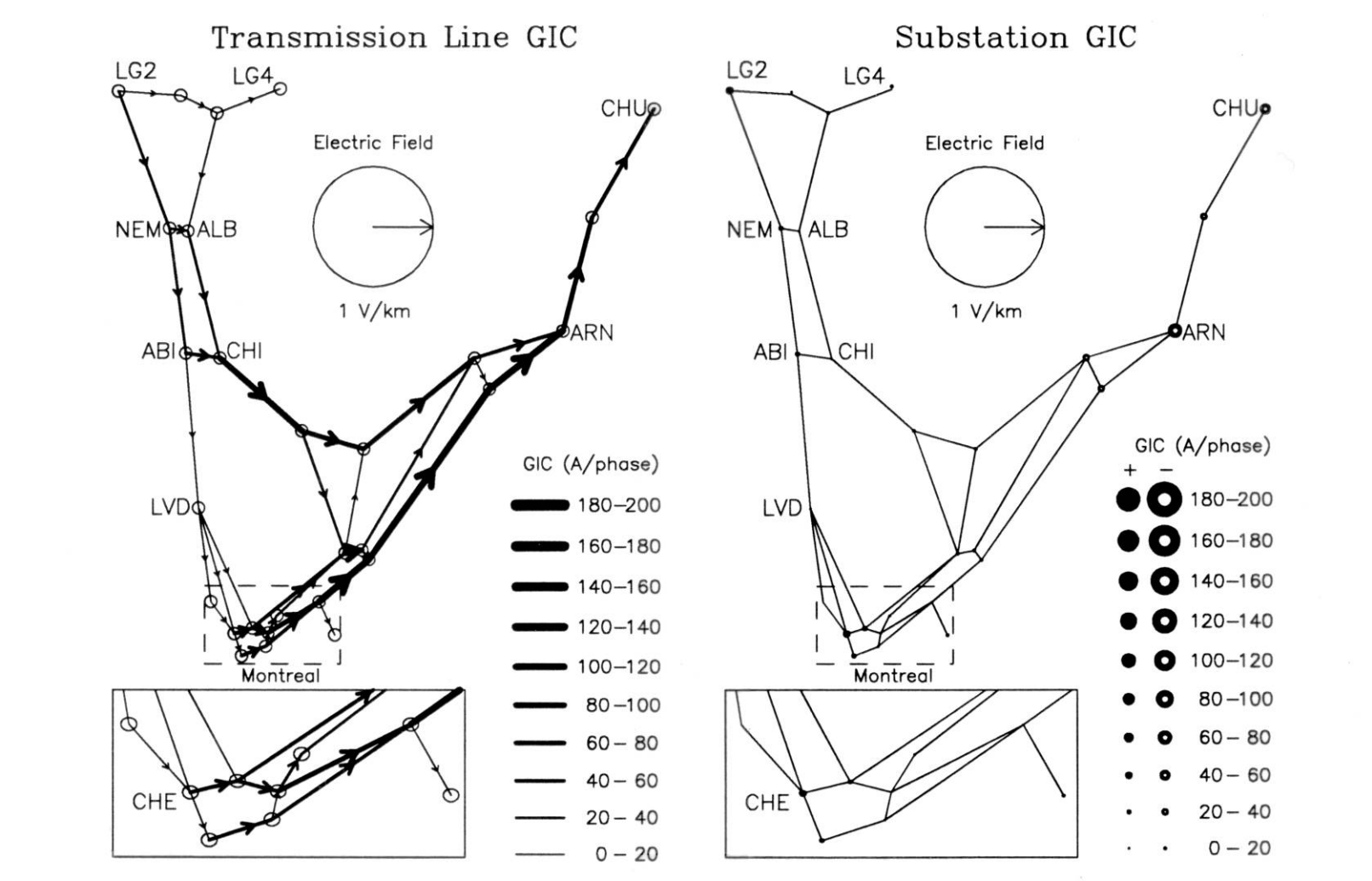
Internet

11:12 PM

# GIC for Northward Electric Field

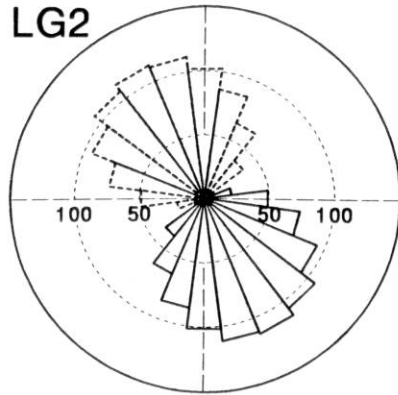


# GIC for Eastward Electric Field

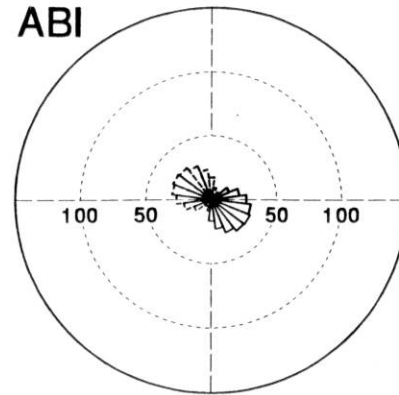


# Directional Sensitivity

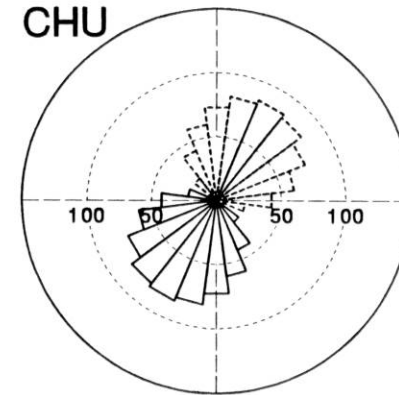
LG2



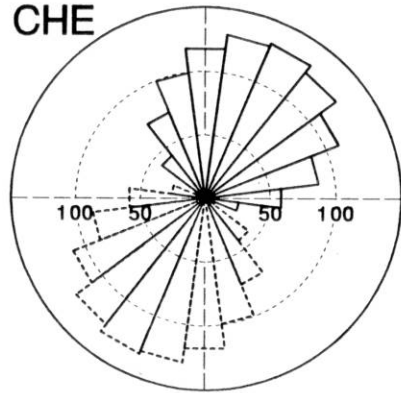
ABI



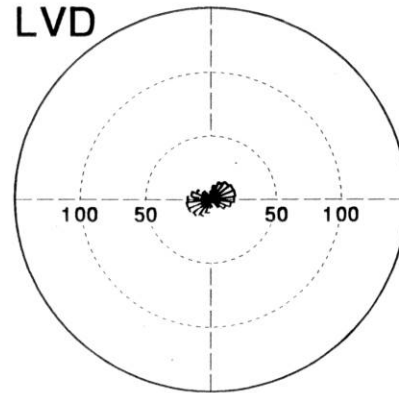
CHU



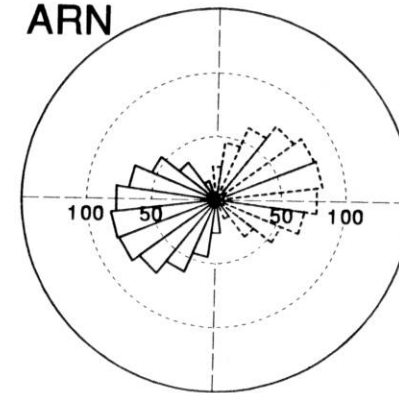
CHE



LVD



ARN



# Impacts on Power System

Spikey waveform → harmonics

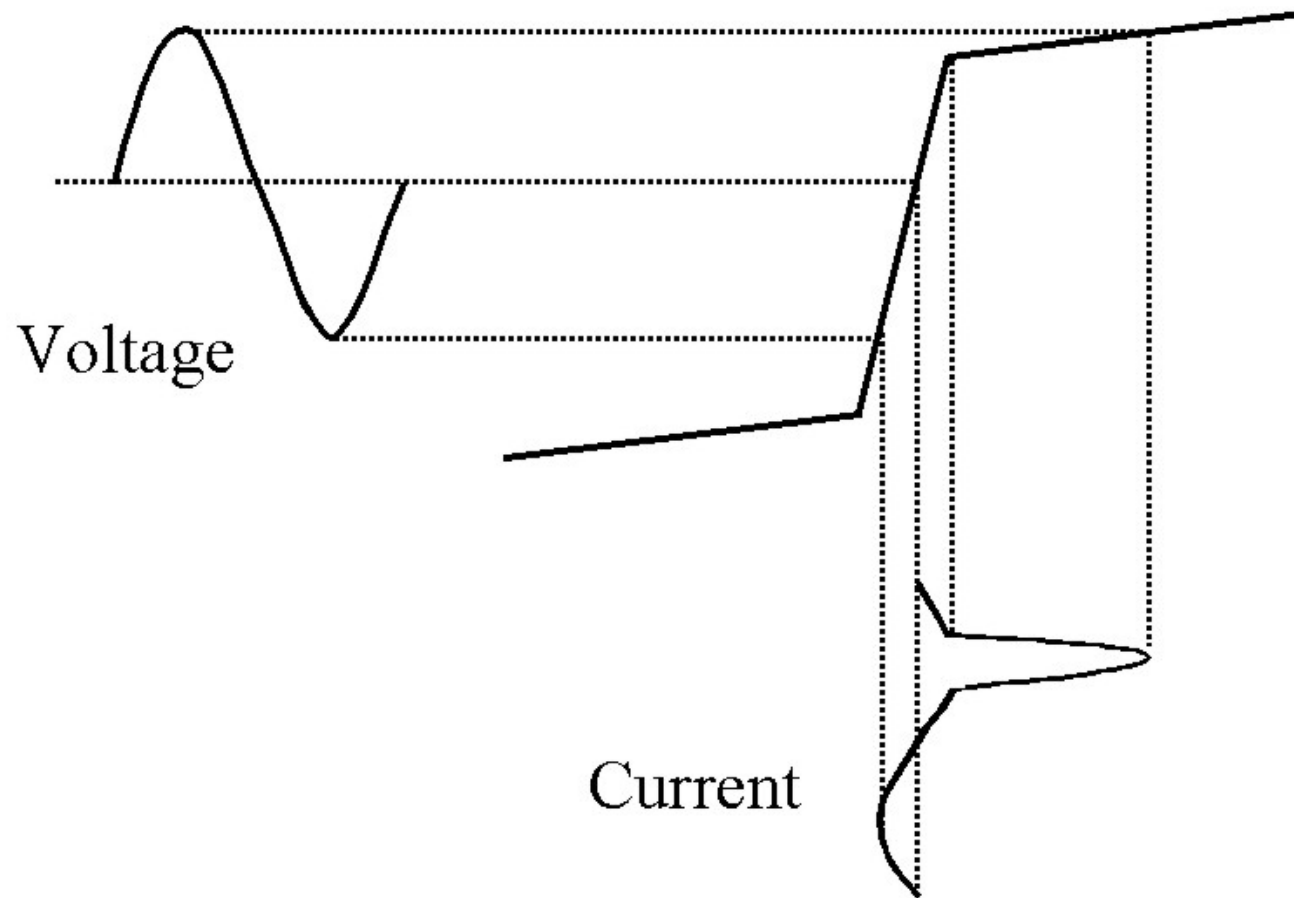
Harmonics cause misoperation of protective relays

Increased magnetising current → increased reactive power consumption

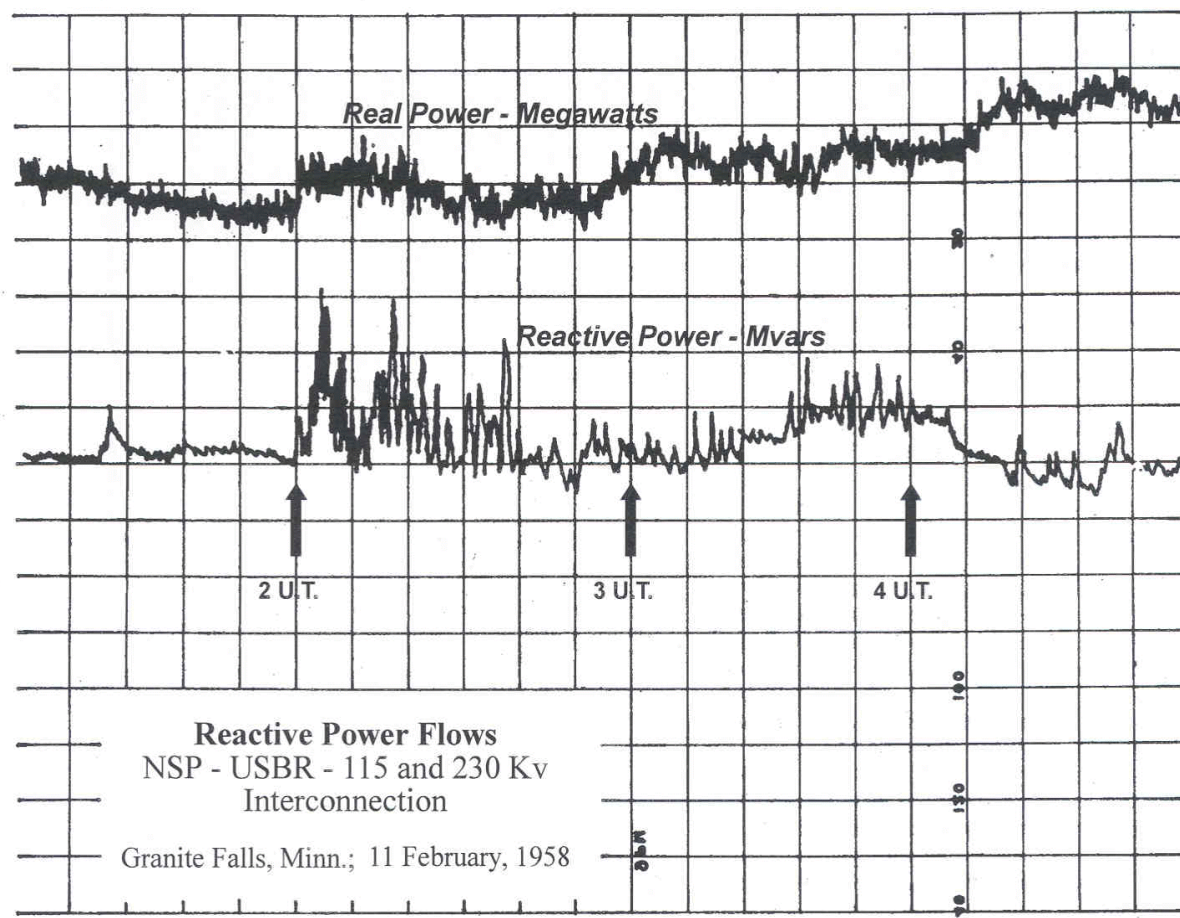
Lack of reactive power causes voltage collapse



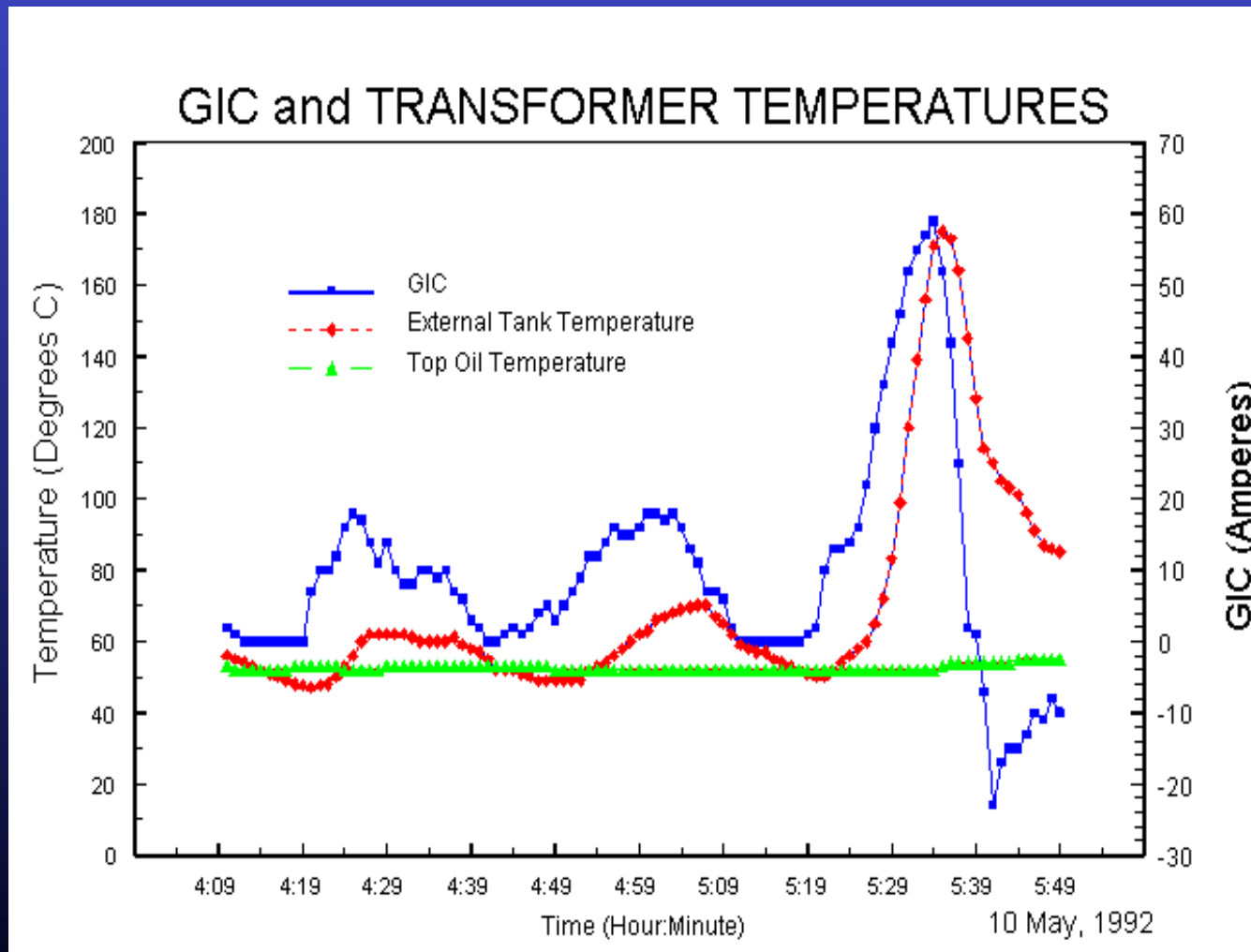
# Power Transformer Hysteresis Curve



# Increased Reactive Power Requirements



# Transformer Overheating



# Conclusions

- Calculation of GIC needs knowledge of geomagnetic disturbance, Earth conductivity, network impedances
- Simulation done assuming:
  - uniform magnetic disturbance
  - 1-D Earth conductivity model
  - resistive network
- Simulation use off-line for hazard assessment and in real-time for system monitoring

**Thank you**

